ENTROPY ON QUASI-METRIC SPACES

PAULUS HAIHAMBO[1,2*] AND OLIVIER OLELA OTAFUDU[1]

[1] *School of Mathematical and Statistical Sciences North-West University, Potchefstroom Campus, Potchefstroom 2520, South Africa*
e-mail: kashitoma@yahoo.com, olivier.olelaotafudu@nwu.ac.za
[2] *Department of Mathematics, University of Namibia*
e-mail: phaihambo@unam.na

Quasi-uniform entropy $h_{QU}(\psi)$ is defined for a uniformly continuous self-map ψ on a quasi-metric space (X, q). Basic properties are proved about this entropy, and it is shown that the quasi-uniform entropy $h_{QU}(\psi, q)$ is less or equal to the Bowen's uniform entropy $h_U(\psi, q^s)$ of ψ considered as a uniformly continuous self-map of the metric space (X, q^s), where q^s is the symmetrised metric of the quasi-metric q. Finally, we prove that the completion theorem for quasi-uniform entropy holds in the class of all join-compact quasi-metric spaces.

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